

AP Calculus AB**Worksheet: Are you Ready?**

1. State the definition of the derivative at $x = a$.

2. State the definition of the derivative function.

3. State three different interpretations of $f'(a)$.

4. $\frac{d}{dx} (f(x))^n = ?$

5. $\frac{d}{dx} [f(x) \cdot g(x)] = ?$

6. $\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = ?$

7. $\frac{d}{dx} (\sin(f(x))) = ?$

8. $\frac{d}{dx} (\cos(f(x))) = ?$

9. $\frac{d}{dx} (\ln(f(x))) = ?$

10. $\frac{d}{dx} e^{f(x)} = ?$

11. $\frac{d}{dx} a^{f(x)} = ?$

12. $\frac{d}{dx} \sin^{-1} f(x) = ?$

13. $\frac{d}{dx} \tan^{-1} f(x) = ?$

14. You are asked to find the limit of a quotient function as x approaches some number a but you get $\frac{0}{0}$. What should you do?

15. The equation of the tangent line to the curve $y = f(x)$ at $x = a$ is given by

What about the equation of the normal line to the same curve at the same point?

16. A function is said to be increasing on an interval if its derivative is

17. State two ways to justify that the graph of a function is concave upward on an interval.

18. You are given that $f'(a) = 0$. State two ways that you can show that $f(a)$ is a local extrema of the curve $y = f(x)$.

19. A function is continuous on the interval $[a, b]$. What do you know about global extrema on the interval? Where must they occur?
20. You are given that a function, f , is continuous on the interval $[a, b]$ and differentiable on the interval (a, b) . You are asked to find the value of c , on (a, b) , that satisfies the conclusion of the Mean Value Theorem. Which c is that?
21. Which three conditions must be met for a function to be continuous at $x = c$?
22. Suppose for a given function, $f(x)$, $f'(a) = 0$ and $f''(a) < 0$. What can you conclude about $f(a)$?
23. Given $\lim_{x \rightarrow \infty} f(x) = 3$. What special feature for the graph of $f(x)$ does this imply?
24. Suppose f is a polynomial function of degree 3 with a positive leading coefficient. If $x = 1$ and $x = 5$ are critical values of f which of the two will produce a local minimum? Why?

25. Suppose you were given a table of function values as illustrated below.

x	a	b	c	d	e
f(x)	f(a)	f(b)	f(c)	f(d)	f(e)

Write an expression that represents the average rate of change of f on $[a, b]$.

How can you approximate the instantaneous rate of change of f at $x = c$?

Suppose f represents a rate of change. Write an expression that approximates the total change of f on $[a, b]$.